

Transmission, tunnelling, reflection

A word on coefficients

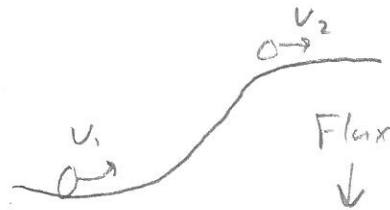
$A \rightarrow \frac{1}{L}$ or # per unit length

$J \rightarrow \frac{\#}{s}$ Flux of probability

$$T = \left| \frac{I}{I} \right|^2, R = \left| \frac{R}{I} \right|^2 = \#$$

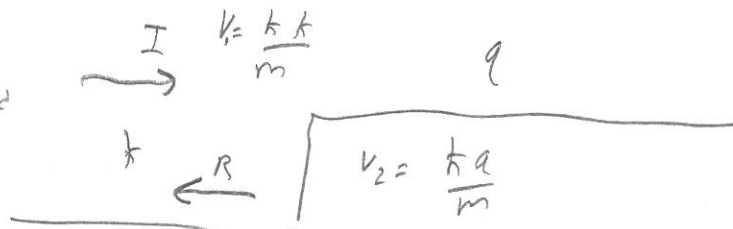
if $v_1 = v_2$ These are probability fluxes

Really $\left| \frac{I}{I} \right|^2 \frac{\hbar k}{m} \cdot \frac{m}{\hbar k}$



if $v_1 \neq v_2 \frac{\hbar k}{m} \neq \frac{\hbar q}{m}$

$$T = \frac{T^2 \frac{q}{m}}{I^2 \frac{k}{m}} = \frac{\#}{\text{second}}$$



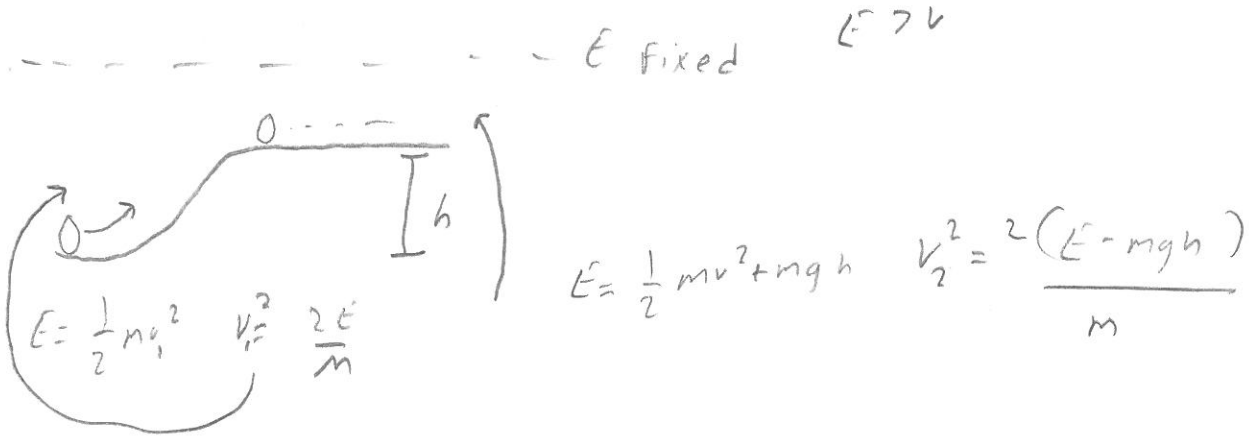
$$-\frac{\hbar^2 \psi''}{2m} = E\psi$$

$$k^2 = -\frac{2mE}{\hbar^2}$$

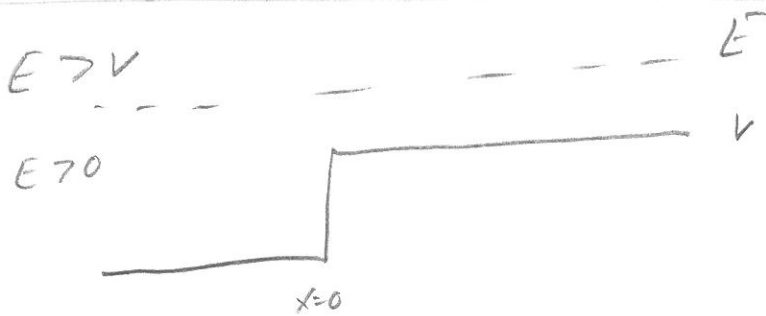
$$-\frac{\hbar^2 \psi''}{2m} + V\psi = E\psi$$

$$q^2 = -\frac{2m}{\hbar^2} (E - V)$$

Bound



If $E < V$



$$-\frac{\hbar^2}{2m} \frac{d^2\psi}{dx^2} = E\psi$$

$$\psi'' = -\frac{2mE}{\hbar^2} \psi$$

$$\psi'' + \frac{2mE}{\hbar^2} \psi = 0$$

$$-\frac{\hbar^2}{2m} \frac{d^2\psi}{dx^2} + V\psi = E\psi$$

$$\psi'' - \frac{2mV}{\hbar^2} \psi = -\frac{2mE}{\hbar^2} \psi$$

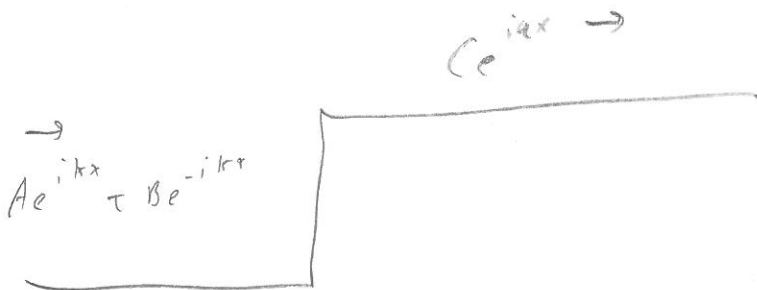
$$\psi'' = \frac{2m}{\hbar^2} (V - E) \psi$$

This is less than zero

$$\#1. \quad \psi_I'' + k^2 \psi_I = 0 \quad k = \frac{\sqrt{2m(E)}}{\hbar} > 0 \quad \psi_I = A e^{ikx} + B e^{-ikx}$$

→
←

$$\#2. \quad \psi_{II}'' + q^2 \psi_{II} = 0 \quad q = \frac{\sqrt{2m(E-V)}}{\hbar} \quad \psi_{II} = C e^{iqx} \quad \text{No reflected wave}$$



$$\psi(0) \rightarrow A+B=C \quad \psi'(0) \quad ik(A-B) = iqC$$

$$R=? \quad ik(A-B) = iq(A+B)$$

$$\frac{k}{q} A - \frac{k}{q} B = A+B$$

$$\left(\frac{k}{q} - 1\right) A = \left(1 + \frac{k}{q}\right) B$$

$$\left(\frac{k-q}{q}\right) A = \left(\frac{k+q}{q}\right) B \quad \frac{B^2}{A^2} \frac{(k-q)^2}{(k+q)^2} = \frac{(k-q)^2}{(k+q)^2} \frac{(k-q)^2}{(k+q)^2}$$

$$= \frac{(k-q)^4}{(k^2 - q^2)^2} = \frac{(\sqrt{E} - \sqrt{E-V})^4}{V^2}$$

$$T = R - 1$$

$$T + R = 1$$

$$E < V$$

$$\psi_I'' + \sqrt{\frac{2mE}{\hbar}} \psi_I = 0 \quad k > 0$$

$$\psi_{II}'' + \sqrt{\frac{2m(V-E)}{\hbar}} \psi_{II} = 0 \quad q > 0$$

$$\psi_I = Ae^{ikx} + Be^{-ikx} \quad \psi_{II} = Ce^{-qx} \quad +qx \text{ diverges}$$



$$\psi(0) \quad \psi'(0)$$

$$A+B=C \quad ik(A-B) = -qC \quad ik(A-B) = -q(A+B)$$

$$\frac{ik}{q}(B-A) = A+B$$

$$\left(\frac{ik}{q} - 1\right)B = \left(1 + \frac{ik}{q}\right)A$$

$$\frac{B}{A} = \frac{1+id}{1-id} \quad \frac{B^2}{A^2} = \frac{(1+id)(1-id)}{(1-id)(1+id)} = 1 \quad A) \text{ reflected}$$

how about

