

Mon: Warm Up

Tues: Discussion / quiz

189, 194, 195, 197, 199, 205, 208

Group Ex Solutions - on D2L

Note  $T_1 + T_2 \neq mg$

$$\begin{array}{ccc} T_1 = 18\text{N} & & T_2 = 34\text{N} \\ & \swarrow & \\ & mg = 44\text{N} & \end{array}$$

because  $18\text{N} + 34\text{N} \neq 44\text{N}$

Quiz 1 95%

Quiz 2 75% - 90%

### Friction

Friction is a force exerted by one surface on another that tends to oppose motion. We will consider two types of friction

- \* kinetic friction ~ surfaces slide relative to each other
- \* static friction ~ surfaces are fixed relative to each other

### Kinetic friction

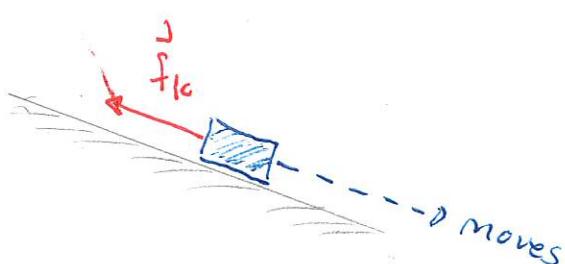
This occurs when one surface moves along the other. This force is denoted  $f_k$  and has properties

- \* direction parallel to surface and opposite to motion
- \* Magnitude

$$f_k = \mu_k n$$

where  $n$  = normal force

$\mu_k$  = coefficient of friction



depends on materials of the surfaces Table 6e1

~~Quiz 3~~ 50% - 75%

~~Quiz 4~~ Quiz 5 :

Note that

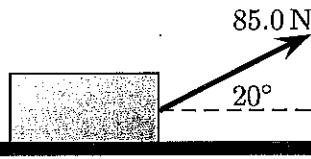
$$f_b = \mu_k n$$

↑ can vary depending on  
circumstances

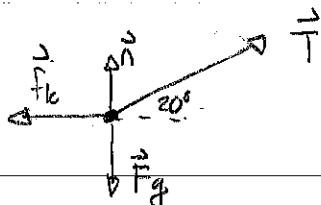
only depends on  
materials

## 192 Dynamics of a single object with friction, 2

A 15.0 kg box moves rightward along a horizontal surface. A rope pulls with a force at the illustrated angle. The coefficient of kinetic friction is 0.350. Use *all of the steps of Newton's Second Law* to determine the acceleration of the box. (131Sp2025)



Answer: ① FBD



② Newton's 2<sup>nd</sup> Law

$$\sum F_{ix} = ma_x$$

$$\sum F_{iy} = ma_y = 0$$

③ Components

$$F_g = mg = 15.0 \text{ kg} \times 9.8 \text{ m/s}^2 = 147 \text{ N}$$

$$f_k = \mu_k n$$

$$T_{ix} = T_i \cos 20^\circ = 85 \text{ N} \cos 20^\circ = 79.9 \text{ N}$$

$$T_{iy} = T_i \sin 20^\circ = 85 \text{ N} \sin 20^\circ = 29.1 \text{ N}$$

	x	y
F <sub>g</sub>	0	-147 N
n	0	n
T	79.9 N	29.1 N
f <sub>x</sub>	-μ <sub>k</sub> n	0

④ Substitute into Newton's 2<sup>nd</sup> Law

$$\sum F_{ix} = ma_x \Rightarrow 79.9 \text{ N} - \mu_k n = ma_x$$

$$\Rightarrow 79.9 \text{ N} - 0.350n = 15.0 \text{ kg } a_x$$

$$\sum F_{iy} = 0 \Rightarrow -147 \text{ N} + n + 29.1 \text{ N} = 0 \Rightarrow n = 118 \text{ N}$$

$$\text{Then } 79.9 \text{ N} - 0.350 \times 118 \text{ N} = 15.0 \text{ kg } a_x$$

$$\Rightarrow 38.6 \text{ N} = 15.0 \text{ kg } a_x \Rightarrow a_x = \frac{38.6 \text{ N}}{15.0 \text{ kg}} \Rightarrow a_x = 2.57 \text{ m/s}^2$$

## Static friction

Static friction occurs when the surfaces do not slide

relative to each other but would in the absence of friction. This is denoted  $\vec{f}_s$  and has properties:

- \* direction = parallel to surface and opposite to motion that would occur
- \* Magnitude = adjustable up to a maximum

$$f_{s\max} = \mu_s n$$

where  $\mu_s$  is the coefficient of static friction (depends on surfaces)

so

$$f_s \leq \mu_s n$$

Quiz 4: 30%

Quiz 6

