

Review I

Thurs: Seminar 12:30
WS 203

Fri: Exam I

Mon: Warm Up 6
Group Exercise

Exam: *Covers Ch 1-4
Lectures 1-11
HW 1-4
Discussion 1-4.

- * Bring: - Calculator - no communicating devices.
- Single 3"x5" card one side.
- * Study - 2022, 2023 Class Exam I - all questions
- HW, Discussion Problems
- Quizzes
- In Class quizzes

10AM Class - Stay in Room until 10:50am.

Ch 1-2 Know - meanings of: displacement, velocity, acceleration
- graphical representations of motion

Equations:

$$\left. \begin{array}{l} v_{avg} = \frac{\Delta x}{\Delta t} \\ v = \text{slope } x \text{ vs } t \\ \Delta x = \text{area under } v \text{ vs } t \end{array} \right\} \left. \begin{array}{l} a_{avg} = \frac{\Delta v}{\Delta t} \\ a = \text{slope } v \text{ vs } t \end{array} \right\} \left. \begin{array}{l} v_f = v_i + a \Delta t \\ y_f = y_i + v_i \Delta t + \frac{1}{2} a \Delta t^2 \\ v_f^2 = v_i^2 + 2a \Delta(x_f - x_i) \end{array} \right\} \begin{array}{l} \text{Free fall} \\ a_y = -g \end{array}$$

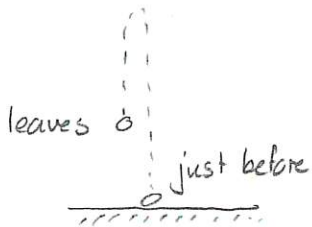
Quiz 1 80% - 100% || 80% - 100% Quiz 2 30% - 30% || 30% - 60%

50 Ball thrown from above the ground ✓

A ball is thrown vertically upwards, leaving the hand at a height of 1.2 m above the ground. It hits the ground 2.5 s after leaving the hand. (131Sp2023)

- a) Determine the speed with which the ball left the hand.
 b) Determine the maximum height above the ground reached by the ball

Answer: a)



$$\begin{aligned}
 t_0 &= 0 \text{ s} & t &= 2.5 \text{ s} \\
 y_0 &= 1.2 \text{ m} & y &= 0 \text{ m} \\
 v_{0y} &= ?? & v_y &= \\
 a_y &= -g = -9.8 \text{ m/s}^2
 \end{aligned}$$

credit!

$$y = y_0 + v_{0y}t + \frac{1}{2}a_y t^2$$

credit!

$$\Rightarrow 0 \text{ m} = 1.2 \text{ m} + v_{0y}(2.5 \text{ s}) + \frac{1}{2}(-9.8 \text{ m/s}^2)(2.5 \text{ s})^2$$

$$\Rightarrow -1.2 \text{ m} = 2.5 \text{ s } v_{0y} - 30.6 \text{ m}$$

$$\Rightarrow 29.4 \text{ m} = 2.5 \text{ s } v_{0y}$$

$$\Rightarrow v_{0y} = \frac{29.4 \text{ m}}{2.5 \text{ s}} = 11.8 \text{ m/s}$$

- b) At max height $v_y = 0$ $y = ??$

$$v_y^2 = v_{0y}^2 + 2a_y(y - y_0)$$

credit!

$$\Rightarrow (0 \text{ m/s})^2 = (11.8 \text{ m/s})^2 + 2(-9.8 \text{ m/s}^2)(y - 1.2 \text{ m})$$

$$\Rightarrow 0 \text{ m}^2/\text{s}^2 = 139 \text{ m}^2/\text{s}^2 - 19.6 \text{ m/s}^2 (y - 1.2 \text{ m})$$

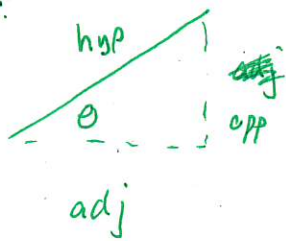
$$\Rightarrow \frac{-139 \text{ m}^2/\text{s}^2}{-19.6 \text{ m/s}^2} = y - 1.2 \text{ m} \Rightarrow y = 7.07 \text{ m} + 1.2 \text{ m}$$

$$\Rightarrow y = 8.3 \text{ m}$$

Ch 3: know - vector algebra

- unit vectors, components

Equations:



$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\vec{A} = A_x \hat{i} + A_y \hat{j}$$

$$A = \sqrt{A_x^2 + A_y^2}$$

Quiz 3

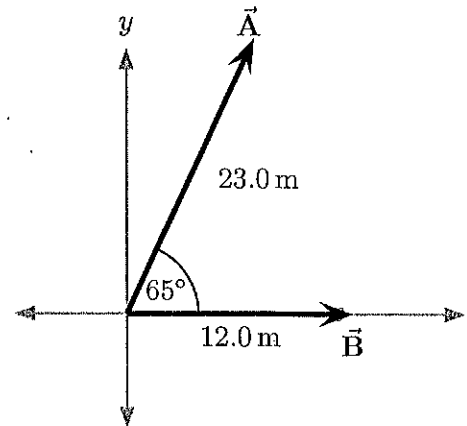
90%

Σ 70% - 90%

134 Vector subtraction, 1

Two displacement vectors, \vec{A} and \vec{B} are illustrated.
(131F2024)

- Determine the components of $\vec{C} = \vec{A} - \vec{B}$.
- Determine the magnitude of \vec{C} .



Answer:

$$\begin{aligned} \text{a) } C_x &= A_x - B_x \\ C_y &= A_y - B_y \end{aligned}$$

Requires components

$$\begin{aligned} A_x &= A \cos 65^\circ \\ &= 23 \text{ m} \cos 65^\circ = 9.7 \text{ m} \end{aligned}$$

$$\begin{aligned} A_y &= A \sin 65^\circ \\ &= 23 \text{ m} \sin 65^\circ = 20.8 \text{ m} \end{aligned}$$

$$C_x = 9.7 \text{ m} - 12.0 \text{ m} = -2.3 \text{ m}$$

$$C_y = 20.8 \text{ m} - 0 \text{ m} = 20.8 \text{ m}$$

	x	y
\vec{A}	9.7 m	20.8 m
B	12.0 m	0 m

$$\begin{aligned} \text{b) } C &= \sqrt{C_x^2 + C_y^2} = \sqrt{(-2.3)^2 + (20.8)^2} \text{ m} \\ &= 21.0 \text{ m} \end{aligned}$$

Ch 4: know - vector vector nature of displacement, velocity, acceleration

Equations :

$$\vec{v} = v_x \hat{i} + v_y \hat{j}$$

\downarrow \downarrow
 $\frac{\Delta x}{\Delta t}$ $\frac{\Delta y}{\Delta t}$

$$\vec{a}_{avg} = \frac{\Delta \vec{v}}{\Delta t}$$

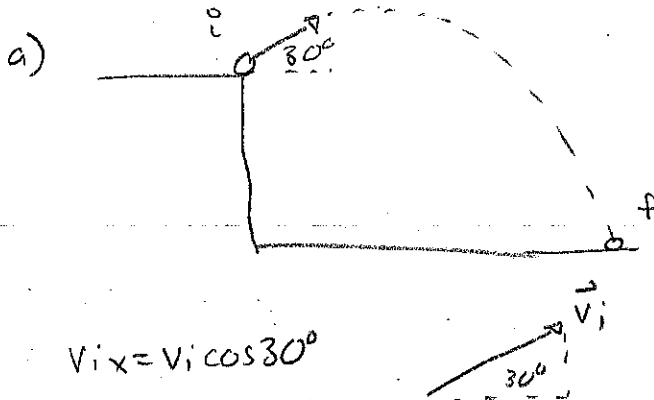
- kinematics eqns (two dimensions)
- projectile $a_x = 0$ $a_y = -g$
- centripetal accel (direction and $a_c = v^2/r$)

Quiz 4 30% - 80% \rightarrow 30% - 90%

135 Ball launched from a cliff

A person hits a ball from the top of a cliff. The ball leaves at height of 12 m above the surface of the water at angle 30° above the horizontal. It hits the water 2.5 s later. (131F2024)

- Determine speed with which the ball is launched.
- Determine the horizontal distance traveled by the ball.



$$v_{ix} = v_i \cos 30^\circ$$

$$v_{iy} = v_i \sin 30^\circ$$

$$t_i = 0 \quad t_f = 2.5 \text{ s}$$

$$x_i = 0 \text{ m} \quad x_f =$$

$$y_i = 12 \text{ m} \quad y_f = 0 \text{ m}$$

$$v_{ix} = v_i \cos 30^\circ$$

$$v_{iy} = v_i \sin 30^\circ$$

$$a_x = 0 \text{ m/s}^2 \quad a_y = -g = -9.8 \text{ m/s}^2$$

Then

$$y_f = y_i + v_{iy} \Delta t + \frac{1}{2} a_y \Delta t^2$$

$$0 = y_i + v_i \sin 30^\circ \Delta t - \frac{1}{2} g \Delta t^2$$

$$\Rightarrow v_i \sin 30^\circ \Delta t = \frac{g}{2} \Delta t^2 - y_i$$

$$\Rightarrow v_i \sin 30^\circ = \frac{g}{2} \Delta t - \frac{y_i}{\Delta t} = \frac{9.8 \text{ m/s}^2 \times 2.5 \text{ s}}{2} - \frac{12 \text{ m}}{2.5 \text{ s}}$$

$$= 12.25 \text{ m/s} - 4.8 \text{ m/s}$$

$$v_i \sin 30^\circ = 7.45 \text{ m/s}$$

$$\Rightarrow v_i = \frac{7.45 \text{ m/s}}{\sin 30^\circ} \Rightarrow v_i = 15 \text{ m/s}$$

$$b) \quad x_f = \cancel{x_i} + v_{ix} \Delta t + \frac{1}{2} \cancel{a_x} \Delta t^2$$

$$x_f = v_i \cos 30^\circ \Delta t$$

$$= 15 \text{ m/s} \cos 30^\circ \times 2.5 \text{ s}$$

$$= 32 \text{ m}$$