

Thurs: Seminar - Cover letter

Fri: Exam I

Mon: Warm Up 6

Exam: * Covers Ch 1, 2, 3, 4

Lectures 1 → 11

HW 1 → 4

Discussion / quiz 1 → 3.

* Bring - calculator (no communicating devices...)

- single 3"x5" card single side.

* Study ~~2018~~, 2018, 2022 Ex I - all questions

- HW

- Discussion probs

- Quizzes

- In-class quizzes

10am class - stay in room until 10:50am

Ch 1 → 3 Know * meanings of: displacement, velocity, acceleration
* graphical representations of motion

Equations:

$v_{avg} = \frac{\Delta x}{\Delta t}$	}	$v = \text{slope } x \text{ vs } t$	}	$v_x = v_{ox} + a_x t$	}	Free fall $a_y = -g$
$a_{avg} = \frac{\Delta v}{\Delta t}$		$a = \text{slope } v \text{ vs } t$		$x = x_0 + v_{ox} t + \frac{1}{2} a_x t^2$		
		$\Delta x = \text{area under } v \text{ vs } t$		$v_x^2 = v_{ox}^2 + 2a_x(x - x_0)$		

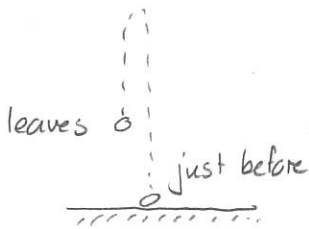
Quiz 1 80% → 90% } 60% → 90%

50 Ball thrown from above the ground

A ball is thrown vertically upwards, leaving the hand at a height of 1.2 m above the ground. It hits the ground 2.5 s after leaving the hand. (131Sp2023)

- Determine the speed with which the ball left the hand.
- Determine the maximum height above the ground reached by the ball!

Answer: a)



$$t_0 = 0 \text{ s} \quad t = 2.5 \text{ s}$$

$$y_0 = 1.2 \text{ m} \quad y = 0 \text{ m}$$

$$v_{0y} = ?? \quad v_y =$$

$$a_y = -g = -9.8 \text{ m/s}^2$$

credit!

$$y = y_0 + v_{0y} t + \frac{1}{2} a_y t^2$$

credit!

$$\Rightarrow 0 \text{ m} = 1.2 \text{ m} + v_{0y} (2.5 \text{ s}) + \frac{1}{2} (-9.8 \text{ m/s}^2) (2.5 \text{ s})^2$$

$$\Rightarrow -1.2 \text{ m} = 2.5 \text{ s } v_{0y} - 30.6 \text{ m}$$

$$\Rightarrow 29.4 \text{ m} = 2.5 \text{ s } v_{0y}$$

$$\Rightarrow v_{0y} = \frac{29.4 \text{ m}}{2.5 \text{ s}} = 11.8 \text{ m/s}$$

b) At max height $v_y = 0$ $y = ??$

$$v_y^2 = v_{0y}^2 + 2 a_y (y - y_0)$$

credit!

$$\Rightarrow (0 \text{ m/s})^2 = (11.8 \text{ m/s})^2 + 2(-9.8 \text{ m/s}^2)(y - 1.2 \text{ m})$$

$$\Rightarrow 0 \text{ m}^2/\text{s}^2 = 139 \text{ m}^2/\text{s}^2 - 19.6 \text{ m/s}^2 (y - 1.2 \text{ m})$$

$$\Rightarrow \frac{-139 \text{ m}^2/\text{s}^2}{-19.6 \text{ m/s}^2} = y - 1.2 \text{ m} \quad \Rightarrow y = 7.07 \text{ m} + 1.2 \text{ m}$$

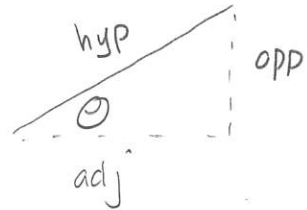
$$\Rightarrow y = 8.3 \text{ m}$$

Ch2: Know * vector algebra

* mit vectors, components

$$\vec{A} = A_x \hat{i} + A_y \hat{j}$$

$$A = \sqrt{A_x^2 + A_y^2}$$



$$\sin \theta = \frac{\text{opp}}{\text{hyp}} \quad \cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

Quiz 2 70% - 90% \rightsquigarrow 50% \rightarrow 90%

63 Vector addition: algebraic method, 2

Two displacement vectors, \vec{A} and \vec{B} are illustrated. Determine the magnitude of $\vec{C} = \vec{A} + \vec{B}$.
(131Sp2023)

We need to find the components of \vec{C}

$$C_x = A_x + B_x$$

$$C_y = A_y + B_y$$

Then the magnitude of \vec{C} is

$$C = \sqrt{C_x^2 + C_y^2}$$

To get the components:

	x	y
\vec{A}	-8.0m	0.0m
\vec{B}	5.0m	-8.66m

$$B_x = B \cos \theta = 10.0m \cos 60^\circ = 5.0m$$

$$B_y = -B \sin \theta = 10.0m \sin 60^\circ = -8.66m$$

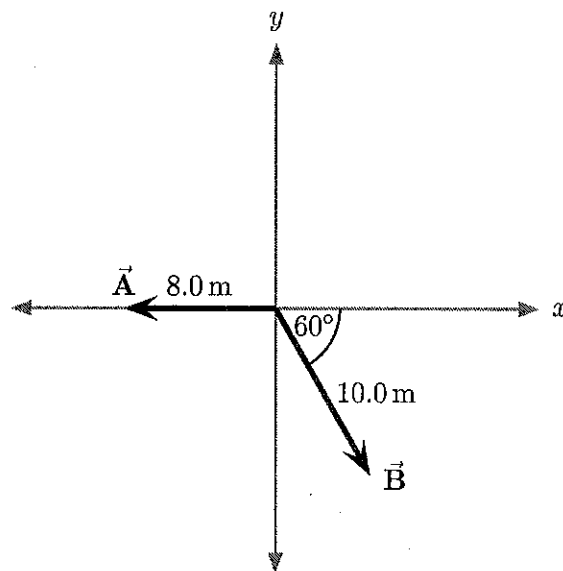
$$\text{So } C_x = -8.0m + 5.0m = -3.0m$$

$$C_y = 0.0m - 8.66m = -8.7m$$

The magnitude is

$$C = \sqrt{(-3.0m)^2 + (-8.7m)^2}$$

$$C = 9.2m$$



Ch4: Know: * vector nature of displacement, velocity, acceleration.

$$* \vec{v} = \frac{\Delta x}{\Delta t} \hat{i} + \frac{\Delta y}{\Delta t} \hat{j}$$

$$* \vec{a}_{\text{avg}} = \frac{\Delta \vec{v}}{\Delta t}$$

* kinematics equations: (two dimensions)

$$* \text{projectile} \quad a_x = 0 \quad a_y = -g$$

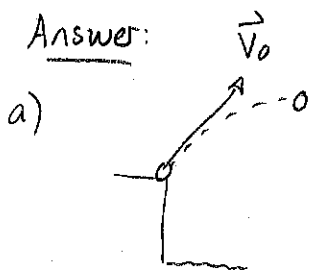
$$* \text{circular motion} \quad a_c = \frac{v^2}{r}$$

Quiz 3 60% - 80% \sum 30% - 40%

103 Stone thrown from a bridge

A person stands on a bridge over a small lake. The person throws a stone with speed 18.0 m/s at an angle of 40° above the horizontal. The stone leaves the hand at a height 3.0 m above the surface of the water.

- Determine the time taken for the stone to reach the highest point in its trajectory.
- Determine the time taken for the stone to hit the water.
- Determine the horizontal distance traveled by the stone between the throw and when it hits the water.

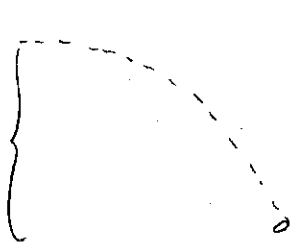


$$\begin{aligned}
 t_0 &= 0 & t &=? \\
 x_0 &= 0\text{m} & x &=? \\
 y_0 &= 3.0\text{m} & y &=? \\
 v_{0x} &= 13.8\text{m/s} & v_x &= \\
 v_{0y} &= 11.6\text{m/s} & v_y &= 0\text{m/s} \\
 a_x &= 0\text{m/s}^2 & a_y &= -9.8\text{m/s}^2
 \end{aligned}$$

$$\begin{aligned}
 v_{0y} &= v_0 \sin 40^\circ \\
 &= 18.0\text{m/s} \sin 40^\circ = 11.6 \\
 v_{0x} &= v_0 \cos 40^\circ = 18\text{m/s} \cos 40^\circ = 13.8
 \end{aligned}$$

$$v_y = v_{0y} + a_y t \Rightarrow \frac{v_y - v_{0y}}{a_y} = t \Rightarrow t = \frac{0\text{m/s} - 11.6\text{m/s}}{9.8\text{m/s}^2} = 1.18\text{s}$$

b) Find additional time for stone to drop \rightarrow requires y from previous part



$$\begin{aligned}
 x_0 &=? \\
 y_0 &=? & y &= 0\text{m} \\
 v_{0x} &= \\
 v_{0y} &= 0\text{m/s} & v_y &=?
 \end{aligned}$$

$$\begin{aligned}
 v_y^2 &= v_{0y}^2 + 2a_y(y - y_0) \\
 0\text{m}^2/\text{s}^2 &= (11.6\text{m/s})^2 - 2 \times 9.8\text{m/s}^2 (y - y_0) \\
 \Rightarrow y - y_0 &= \frac{-(11.6\text{m/s})^2}{19.6\text{m/s}^2} = 6.87\text{m} \\
 \Rightarrow y &= 3.0\text{m} + 6.87\text{m} \\
 &= 9.87\text{m}
 \end{aligned}$$

~~is~~ This is the new y_0 .

$$\text{Then: } y = y_0 + v_{0y}t + \frac{1}{2}a_y t^2$$

$$\Rightarrow 0\text{m} = 9.87\text{m} - \frac{1}{2}(9.8\text{m/s}^2)t^2 \Rightarrow t = \sqrt{\frac{2 \times 9.87\text{m}}{9.8\text{m/s}^2}}$$

$$= 1.42\text{s}$$

The total travel time is $1.18\text{s} + 1.42\text{s} = 2.6\text{s}$

c)



$$t_0 = 0\text{s} \quad t = 2.6\text{s}$$

$$x_0 = 0\text{m} \quad x = ?$$

$$v_{0x} = 13.8\text{m/s} \quad v_x = ?$$

$$a_x = 0\text{m/s}^2$$

$$x = x_0 + v_{0x}t + \frac{1}{2}a_x t^2 \Rightarrow x = 13.8\text{m/s} \times 2.6\text{s} = 35.9\text{m}$$