

Mon: Exam 2 - 50 min in class

Covers: Ch 3.7, 4, 5, 6

Lectures 13-21

HW 4-6

Bring: * Calculator (not communicating device)

* First Index Card.

* Second Index Card \rightarrow 3" x 5" single sided card.

Study: * 2016, 2019 Exam 2 - all questions

* HW, Discussion problems

* Class quizzes

* Concept Tests

Ch 4, 5

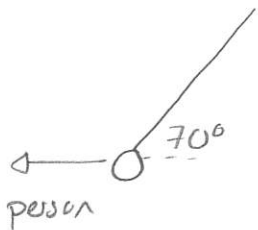
$$\vec{F}_{\text{net}} = m\vec{a} \quad \sum F_{ix} = ma_x \quad \sum F_{iy} = ma_y \quad w = mg$$

$$f_{s \text{ max}} = \mu_s n \quad f_k = \mu_k n \quad \text{Newton's Third Law}$$

Quiz 1 40% - 80%

129 Suspended ball

A 6.0 kg ball is suspended from the ceiling. A person pushes horizontally on the ball so that the ball is at rest with the rope at an angle of 70° from the horizontal. Determine the force exerted by the person. (111F2023)



magnitudes

$$W = Mg = 6.0 \text{ kg} \times 9.8 \text{ m/s}^2 = 59 \text{ N}$$

components

$$T_x = T \cos 70^\circ$$

$$T_y = T \sin 70^\circ$$

Thus:

$$\sum F_{ix} = 0 \Rightarrow -F_{\text{person}} + T \cos 70^\circ = 0$$

$$\Rightarrow F_{\text{person}} = T \cos 70^\circ$$

$$\sum F_{iy} = 0 \Rightarrow -59 \text{ N} + T \sin 70^\circ = 0 \Rightarrow T \sin 70^\circ = 59 \text{ N}$$

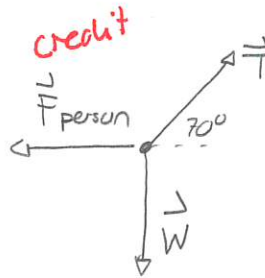
$$\Rightarrow T \times 0.94 = 59 \text{ N}$$

$$\Rightarrow T = 59 \text{ N} / 0.94 = 63 \text{ N}$$

$$\text{Thus } F_{\text{person}} = 63 \text{ N} \cos 70^\circ$$

$$= 63 \text{ N} \times 0.34 = 21 \text{ N} \Rightarrow F_{\text{person}} = 21 \text{ N}$$

FBD



Newton's 2nd Law

$$\sum F_{ix} = M a_x = 0$$

$$\sum F_{iy} = M a_y = 0$$

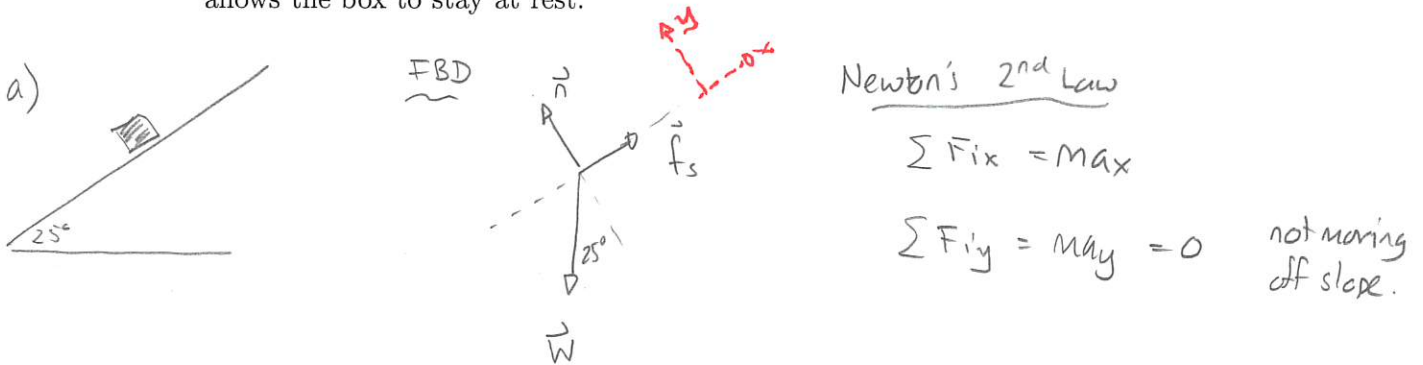
credit.

	x	y
W	0	-59N
F _{person}	-F _{person}	0
T	T cos 70°	T sin 70°

167 Box on a ramp

A 100 kg box is at rest on a ramp that is inclined at angle 25° from the horizontal. (111F2023)

- Determine the friction force on the box.
- Determine the minimum coefficient of static friction between the box and ramp that allows the box to stay at rest.



magnitudes

$$W = mg = 100 \text{ kg} \times 9.8 \text{ m/s}^2 = 980 \text{ N}$$

$$f_s = \mu_s n$$

components

$$W_x = -W \sin 25^\circ = -980 \text{ N} \sin 25^\circ = -414 \text{ N}$$

$$W_y = -W \cos 25^\circ = -980 \text{ N} \cos 25^\circ = -890 \text{ N}$$

	x	y
\vec{W}	-414 N	-890 N
\vec{n}	0	n
\vec{f}_s	f_s	0

Newton's 2nd Law

$$\sum F_{ix} = 0 \Rightarrow -414 \text{ N} + f_s = 0 \Rightarrow f_s = 414 \text{ N}$$

$$\sum F_{iy} = 0 \Rightarrow -890 \text{ N} + n = 0 \Rightarrow n = 890 \text{ N}$$

$$f_s = \mu_s n \Rightarrow 414 \text{ N} = \mu_s 890 \text{ N} \Rightarrow \mu_s = \frac{414 \text{ N}}{890 \text{ N}} = 0.46$$

$$\mu_s = 0.46$$

Ch 3.7, 6

uniform circular motion

$$\vec{a} \text{ inward} \quad a = \frac{v^2}{r}$$

$$T = 1/f \quad v = \frac{2\pi r}{T}$$

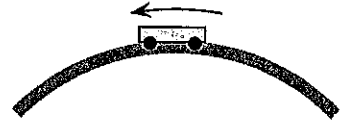
} gravitation

$$F_{\text{grav}} = G \frac{m_1 m_2}{r^2}$$

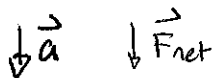
Quiz 2 50%

203 Cart sliding over a hill

A 30 kg cart slides over a hill, which has a circular cross-section of radius 12 m. The speed of the cart at the highest point is 4.0 m/s. Determine the normal force exerted by the hill on the cart. (111F2023)



Ans: FBD



Newton's 2nd Law

$$\sum F_{iy} = ma_y$$

$$a = \frac{v^2}{r}$$

$$a = \frac{(4.0 \text{ m/s})^2}{12} = 1.33 \text{ m/s}^2$$

magnitudes

$$W = mg = 30 \text{ kg} \times 9.8 \text{ m/s}^2 = 294 \text{ N}$$

Components, etc,

$$\sum F_{iy} = ma_y \Rightarrow n - w = -m(1.33 \text{ m/s}^2)$$

$$\Rightarrow n - 294 \text{ N} = -30 \text{ kg} \times 1.33 \text{ m/s}^2$$

$$= -40 \text{ N}$$

$$\Rightarrow n = 294 \text{ N} - 40 \text{ N}$$

$$\Rightarrow n = 254 \text{ N}$$