

Monday

Class Exam 1: Mon, Sept 18 in class
50 minutes.

Covers: Ch 1-3

Lectures 1-12

Discussions 1-3

HW 1-3

Bring: * Calculator (no communicating devices)

* Single 3" x 5" card / sheet single side.

* Study: PROBLEMS!

- 2016, 2019 Class Ex 1 all questions
- HW questions
- Discussion questions
- Quizzes
- In-class quizzes

Ch 1, Ch 2 Motion in one dimension

$$v_{avg} = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{t_f - t_i}$$

$$a_{avg} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i}$$

 $v = \text{slope } x \text{ vs } t$
 $v > 0 \Rightarrow \text{right}$
 $v < 0 \Rightarrow \text{left}$
 $a = \text{slope } v \text{ vs } t$

$$v_f = v_i + a \Delta t$$

$$x_f = x_i + v_i \Delta t + \frac{1}{2} a (\Delta t)^2$$

$$v_f^2 = v_i^2 + 2a_y(y_f - y_i)$$

Free fall

$$a = -g = -9.80 \text{ m/s}^2$$

Quiz 1 type in option f 20% - 40%

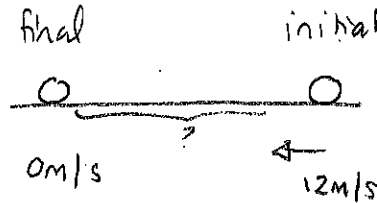
Quiz 2 30 - 60%

48 Reversing cart

At an initial instant a cart travels to the left with speed 12 m/s. Subsequently the cart's acceleration is 4.0 m/s². (111F2023)

- How long does it take for the cart to reverse its direction of travel?
- How far does the cart travel before it reverses its direction of travel?

Answer: a)



$$\begin{aligned} t_i &= 0 \text{ s} & t_f &= \\ x_i &= 0 \text{ m} & x_f &= \\ v_i &= -12 \text{ m/s} & v_f &= 0 \text{ m/s} \end{aligned}$$

$$a = 4.0 \text{ m/s}^2$$

$$v_f = v_i + a \Delta t \Rightarrow 0 \text{ m/s} = -12 \text{ m/s} + 4.0 \text{ m/s}^2 \Delta t$$

$$\Rightarrow 12 \text{ m/s} = 4.0 \text{ m/s}^2 \Delta t$$

$$\Rightarrow \frac{12 \text{ m/s}}{4.0 \text{ m/s}^2} = \Delta t \Rightarrow \Delta t = 3.0 \text{ s}$$

$$b) \quad x_f = x_i + v_i \Delta t + \frac{1}{2} a_x (\Delta t)^2$$

$$= 0 \text{ m} - 12 \text{ m/s} \times 3.0 \text{ s} + \frac{1}{2} (4.0 \text{ m/s}^2) (3.0 \text{ s})^2$$

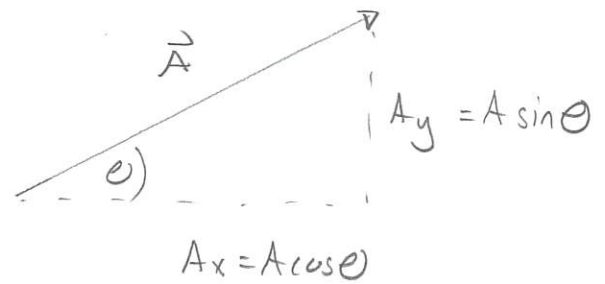
$$= -36 \text{ m} + 18 \text{ m}$$

$$= -18 \text{ m}$$

It moves 18 m to the left.

Ch3 Vectors, motion in two dimensions

Know: vector addition
vector components



velocity vector

- * magnitude \equiv speed
- * direction \equiv tangent to trajectory.

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

$$v_{fx} = v_{ix} + a_x \Delta t$$

$$x_f = x_i + v_{ix} \Delta t + \frac{1}{2} a_x (\Delta t)^2$$

$$v_{fx}^2 = v_{ix}^2 + 2a_x(x_f - x_i)$$

$$v_{fy} = v_{iy} + a_y \Delta t$$

$$y_f = y_i + v_{iy} \Delta t + \frac{1}{2} a_y (\Delta t)^2$$

$$v_{fy}^2 = v_{iy}^2 + 2a_y(y_f - y_i)$$

Projectiles



$$a_x = 0 \text{ m/s}^2$$

$$a_y = -9.8 \text{ m/s}^2$$

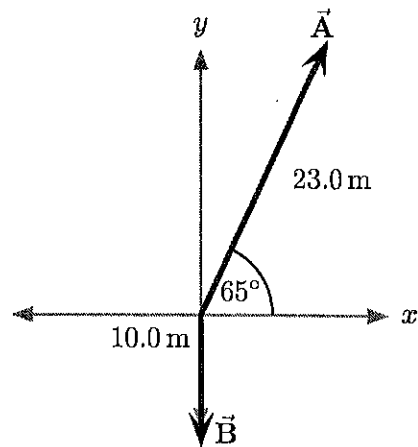
Quiz 3

Quiz 4 40% - 90%

74 Vector addition: algebraic method, 4

Two displacement vectors, \vec{A} and \vec{B} are illustrated.
(111F2023)

- Determine the components of $\vec{C} = \vec{A} + \vec{B}$.
- Determine the magnitude of \vec{C} .



Answer: Need components of \vec{A}, \vec{B}

$$A_x = A \cos 65^\circ = 23.0 \text{ m} \cos 65^\circ \\ = 9.7 \text{ m}$$

$$A_y = A \sin 65^\circ = 23.0 \text{ m} \sin 65^\circ \\ = 21 \text{ m}$$

$$B_x = 0 \text{ m}$$

$$B_y = -10 \text{ m}$$

$$C_x = A_x + B_x = 9.7 \text{ m} + 0 \text{ m} = 9.7 \text{ m}$$

$$C_y = A_y + B_y = 21 \text{ m} - 10 \text{ m} = 11 \text{ m}$$

$$b) \quad C = \sqrt{C_x^2 + C_y^2} = \sqrt{(9.7 \text{ m})^2 + (11 \text{ m})^2} = 15 \text{ m}$$

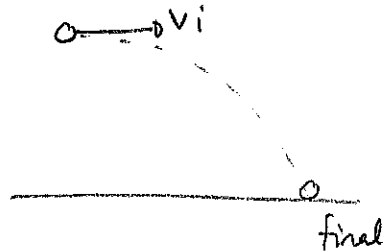
95 Ball thrown horizontally

A ball is thrown, leaving the hand horizontally at a height of 2.0 m above the ground. It lands a horizontal distance of 5.0 m from where it left the hand. (111F2023)

- Determine the time from when the ball leaves the hand until it hits the ground.
- Determine the speed with which the ball leaves the hand.

Answer

a)



$$t_i = 0 \text{ s}$$

$$t_f =$$

$$x_i = 0 \text{ m}$$

$$x_f = 5.0 \text{ m}$$

$$y_i = 2.0 \text{ m}$$

$$y_f = 0 \text{ m}$$

$$v_{ix} =$$

$$v_{fx} =$$

$$v_{iy} = 0 \text{ m/s}$$

$$v_{fy} =$$

$$a_x = 0 \text{ m/s}^2$$

$$a_y = -9.8 \text{ m/s}^2$$

$$y_f = y_i + v_{iy} \Delta t + \frac{1}{2} a_y (\Delta t)^2$$

$$0 \text{ m} = 2.0 \text{ m} + \cancel{0 \text{ m/s}} \Delta t + \frac{1}{2} (-9.80 \text{ m/s}^2) (\Delta t)^2$$

$$-2.0 \text{ m} = -4.90 \text{ m/s}^2 (\Delta t)^2$$

$$(\Delta t)^2 = \frac{2.0 \text{ m}}{4.90 \text{ m/s}^2} = 0.41 \text{ s}^2 \quad \Rightarrow \Delta t = \sqrt{0.41 \text{ s}^2} \quad \Rightarrow \Delta t = 0.64 \text{ s}$$

$$b) \quad x_f = x_i + v_{ix} \Delta t + \frac{1}{2} a_x (\Delta t)^2$$

$$5.0 \text{ m} = v_{ix} 0.64 \text{ s}$$

$$v_{ix} = \frac{5.0 \text{ m}}{0.64 \text{ s}} \Rightarrow$$

$$v_{ix} = 7.8 \text{ m/s}$$