

## Intermediate Laboratory: Homework 3

Due: 4 February 2019

Read chapter 4 and complete the following problems.

- 1 Taylor, *Error Analysis*, 4.2, page 111.
- 2 Taylor, *Error Analysis*, 4.6, page 111.
- 3 Taylor, *Error Analysis*, 4.16, page 114.
- 4 Taylor, *Error Analysis*, 4.18, page 115.
- 5 Taylor, *Error Analysis*, 4.20, page 115.
- 6 Taylor, *Error Analysis*, 4.24, page 116.

### 7 Statistical Analysis of Random Numbers

Excel has a random number generator and we can use this to explore the statistics of sampling distributions. The Excel function RAND() returns a number between  $0 \leq x \leq 1$  and it is claimed that the distribution which governs this is uniform (i.e. each number is equally likely). One can show that the (true) mean of this distribution is  $\frac{1}{2}$  and the (true) standard deviation is  $\frac{1}{\sqrt{12}}$ .

Set up an Excel spreadsheet. Create a column of 20 randomly generated numbers; this forms one “data set.”

- a) Determine the sample average of the numbers in the single data set and their standard deviation. Are these similar to the true mean and true standard deviation?

Repeat the above procedure 15 times (copy the original column). You will have 15 data sets.

- b) For each data set obtain the sample average and standard deviation (call this  $\sigma$ ). Do these fluctuate from one data set to another? If so, what are their ranges?
- c) Now consider the 15 sample averages as a single set of data. Determine the average and standard deviation (call this  $\sigma_{\text{averages}}$ ) of all of these sample averages. Does the true mean lie within this range? How does  $\sigma_{\text{averages}}$  compare to the various  $\sigma$  that each data set yielded?
- d) For each data set, determine the standard deviation of the mean (call this  $\sigma_{\text{mean}}$ ). How does it compare to  $\sigma_{\text{averages}}$ ? Which of  $\sigma$  or  $\sigma_{\text{mean}}$  more accurately reflects the fluctuations in the sample averages,  $\sigma_{\text{averages}}$ ?

- e) Treat all of the data points as one set. Determine the average and standard deviation of these. Is the standard deviation over the 300 data points much different to that over any single set of 20 data points?
- f) Which better reflects the uncertainty in a sample average: the standard deviation or the standard deviation of the mean?