

Lecture 8Weds / Thurs LABS - prelabFri: HW due by 5pm

Supp Ex 29, 30, 31, 32, 33a

Ch 21 Q 5

Prob 19, 79

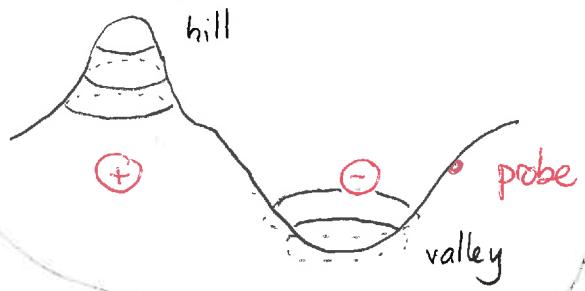
Fri: Physics candidate seminar WS 264Energy in electrostatics

The basic scheme regarding energy in electrostatics is:

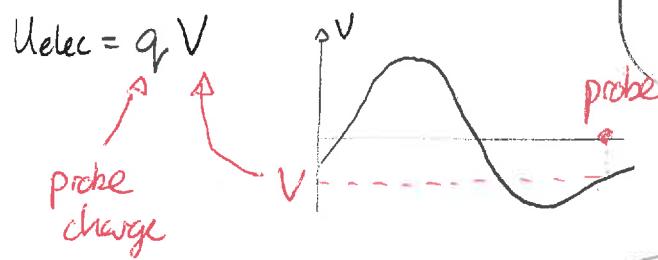
Probe in the vicinity of sources. Speed of prob?

Sources establish electric potential, V :

- * one value at each location
- * energy "landscape"



Probe placed in landscape has electric potential energy



→ Conservation of energy
 $\Delta K + \Delta U_{elec} = 0$

Demo: PhET Charges + fields

- Place various charges - observe red/blue
 - use meter to observe V
 - describe hills/valleys

Demo: Video Khutoryansky : 0:27, 0:59, 1:50

Quiz 1 20% - 50%

Recall that the electric potential only depends on the arrangement of source charges.

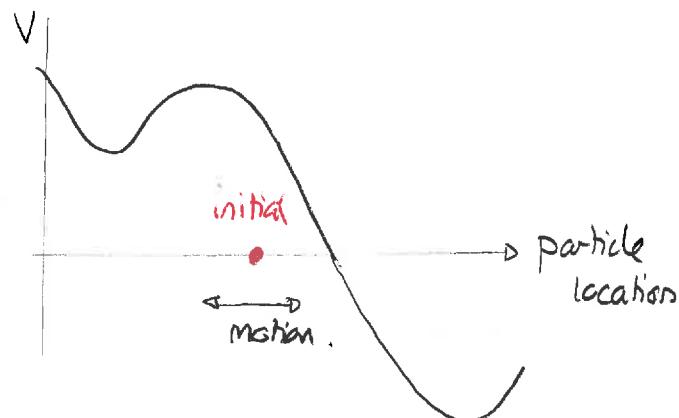
Motion of a probe in an electric potential

Consider the situation where a collection of hidden sources produces an electric potential as illustrated. Suppose that a probe can move along one line.

At an initial instant the particle is given a kick either left or right. How does the potential describe its subsequent motion?

Here

$$\begin{aligned}\Delta K + \Delta U_{elec} &= 0 \\ \Rightarrow \Delta K + q_i \Delta V &= 0 \\ \Rightarrow \Delta K &= -q_i \Delta V\end{aligned}$$



where q_i is the probe charge. We can now observe how V changes.

The key factors are:

- * Is ΔV positive, negative? } What does this say
- * Is q_i " " ? } about ΔK .

Quiz 2 - 50% \rightarrow 90%

We see that

- | | |
|---|-----------------------------|
| A positive probe speeds up when moving down V | " " " slows down " " up V |
| A negative " speeds up " " up V | A " " slows down " " down V |

Quiz 3

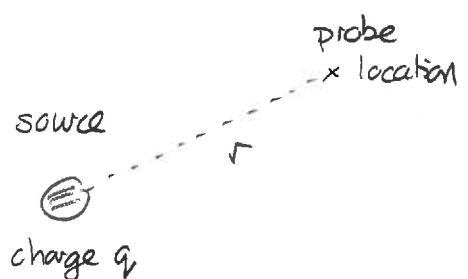
Note that the sign of the potential is important.

Potential produced by a point charge

So far we have not described how to determine the potential produced by sources. The simplest case involves a point charge. The way to determine the potential involves using calculus to determine the work done on a probe as it moves from one location to another. This gives ΔU_{elec} and eventually ΔV . The result is:

The electric potential produced at a point a distance r from a source charge is

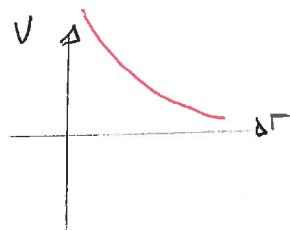
$$V = k \frac{q}{r}$$



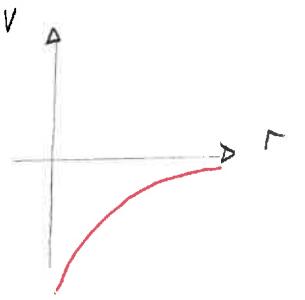
where q is the charge of the source charge

Quiz 4 30% → 90%

Graphing gives the following:



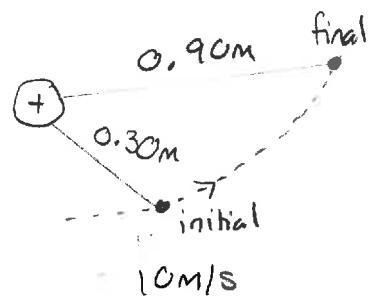
positive source



negative source

Example: A point particle with charge $+4.0 \times 10^{-6} C$ is held fixed

A probe charge with mass 0.060 kg and charge $8.0 \times 10^{-6} C$ moves as illustrated. Determine its speed at the final location.



Answer: Energy conservation

$$\Delta K + \Delta U_{\text{elec}} \Rightarrow \Delta K + q_{\text{probe}} \Delta V = 0$$

$$\Delta K = - q_{\text{probe}} \Delta V$$

$$\frac{1}{2} M V_f^2 - \frac{1}{2} M V_i^2 = - q_{\text{probe}} (V_f - V_i)$$

We need initial and final potentials.

$$V_i = k \frac{q_{\text{source}}}{r_i} = \frac{8.99 \times 10^9 \text{ Nm}^2/\text{C}^2 \times 4.0 \times 10^{-6} \text{ C}}{0.30 \text{ m}} = 120000 \text{ V}$$

$$V_f = k \frac{q_{\text{source}}}{r_f} = \frac{8.99 \times 10^9 \text{ Nm}^2/\text{C}^2 \times 4.0 \times 10^{-6} \text{ C}}{0.90 \text{ m}} = 40000 \text{ V}$$

So

$$\begin{aligned} \frac{1}{2} M V_f^2 - \frac{1}{2} M V_i^2 &= - 8.0 \times 10^{-6} \text{ C} [40000 \text{ V} - 120000 \text{ V}] \\ &= + 0.64 \text{ J} \end{aligned}$$

$$\frac{1}{2} (0.0060\text{kg}) v_f^2 - \frac{1}{2} (0.0060\text{kg}) (10\text{m/s})^2 = +0.64\text{J}$$

$$0.0030\text{kg} v_f^2 - 0.30\text{J} = 0.64\text{J}$$

$$\Rightarrow 0.0030\text{kg} v_f^2 = 0.94\text{J}$$

$$\Rightarrow v_f^2 = 313\text{m}^2/\text{s}^2$$

$$\Rightarrow v_f = \sqrt{313\text{m}^2/\text{s}^2} = 18\text{m/s}$$